

# Genetic Programming: Language and Representation

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# Previous Lecture

- ❖ How to make tree GP more expressive

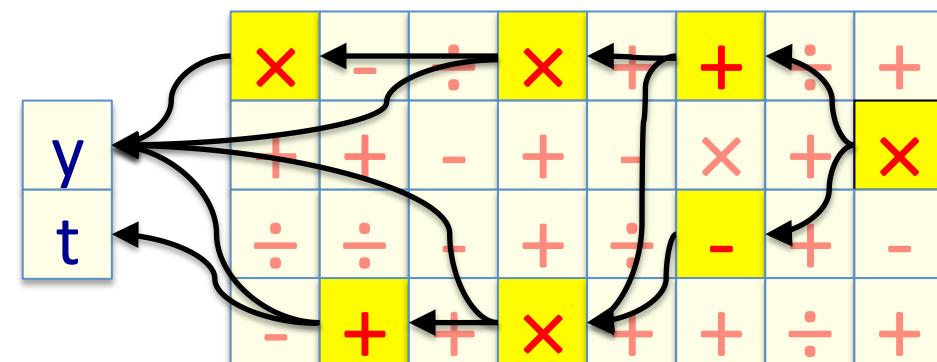
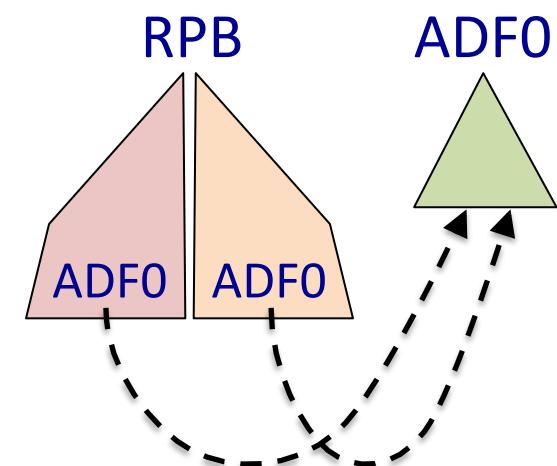
- ▷ Memory, iteration and modularity

- ❖ Approaches to modularity in GP

- ▷ ADFs
- ▷ Refactoring mutations
- ▷ Analytical approaches

- ❖ Cartesian GP

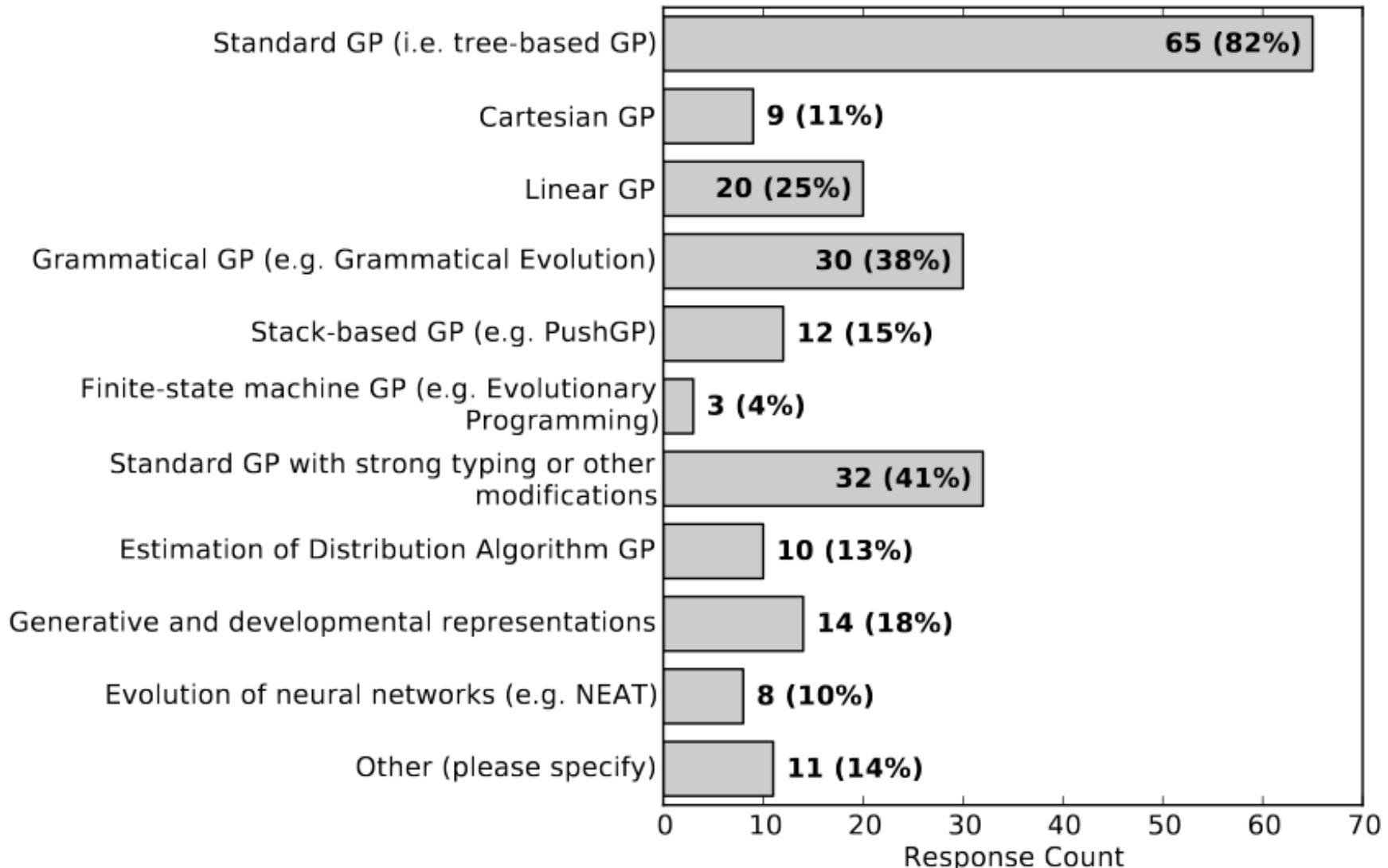
- ▷ Graph-based GP
- ▷ Role of redundancy



# Today's Lecture

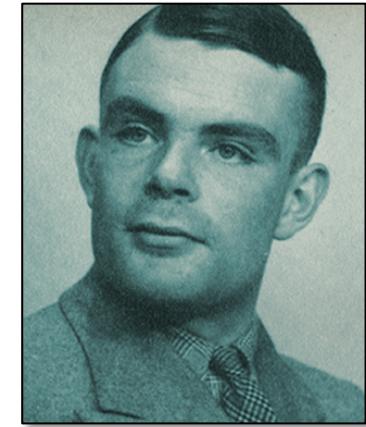
- ◊ Other ways of representing programs
  - ▷ Linear GP: lists of instructions
  - ▷ Grammatical evolution: lists of grammar transitions
- ◊ Developmental genetic programming
  - ▷ Growing programs and other structures
  - ▷ Transitioning between representations
  - ▷ Addressing scalability
  - ▷ Computing more like biology

# GP Community Survey



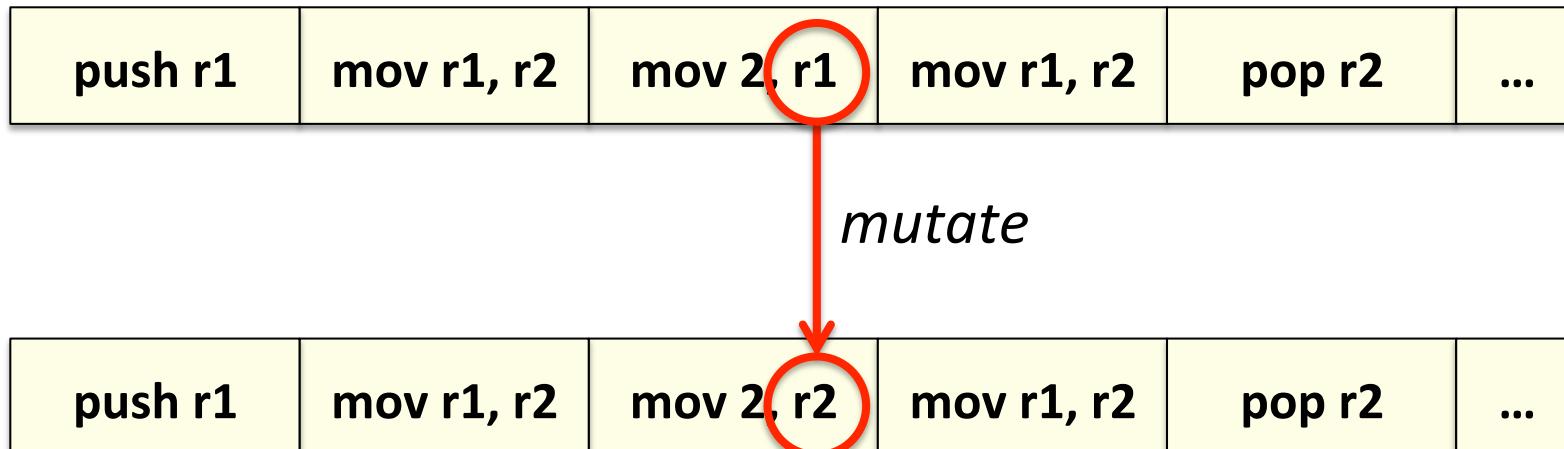
# Real Languages?

- ❖ Tree GP doesn't use standard languages
  - ▷ Requires special interpreters
  - ▷ Challenging to integrate with existing code
  - ▷ Typically not Turing-complete
  - ▷ Language features appear a little *ad hoc*
  
- ❖ Other approaches do use conventional languages
  - ▷ Machine languages (e.g. x86 assembler): **Linear GP**
  - ▷ Imperative languages (e.g. C): **Grammatical evolution**
  - ▷ Functional languages (e.g. Haskell): PolyGP
  - ▷ Logic languages (e.g. Prolog): DCTG-GP



# Linear GP

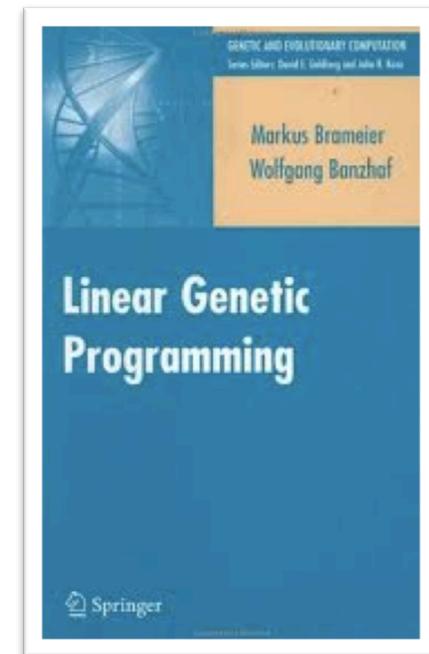
- ◊ Evolves lists of machine language instructions
  - ▷ So, works a lot like a genetic algorithm
  - ▷ Variation operators less likely to break syntax
  - ▷ Often no need for an interpreter or a compiler
  - ▷ However, semantic (e.g. runtime) errors are possible



# Linear GP

◊ Languages that have been targeted include:

- ▷ Sun SPARC assembler (RISC)
- ▷ Intel i386 assembler (CISC)
- ▷ Java bytecode
- ▷ CUDA instructions
- ▷ Novel hardware languages
- ▷ GP-specific languages, e.g. Push

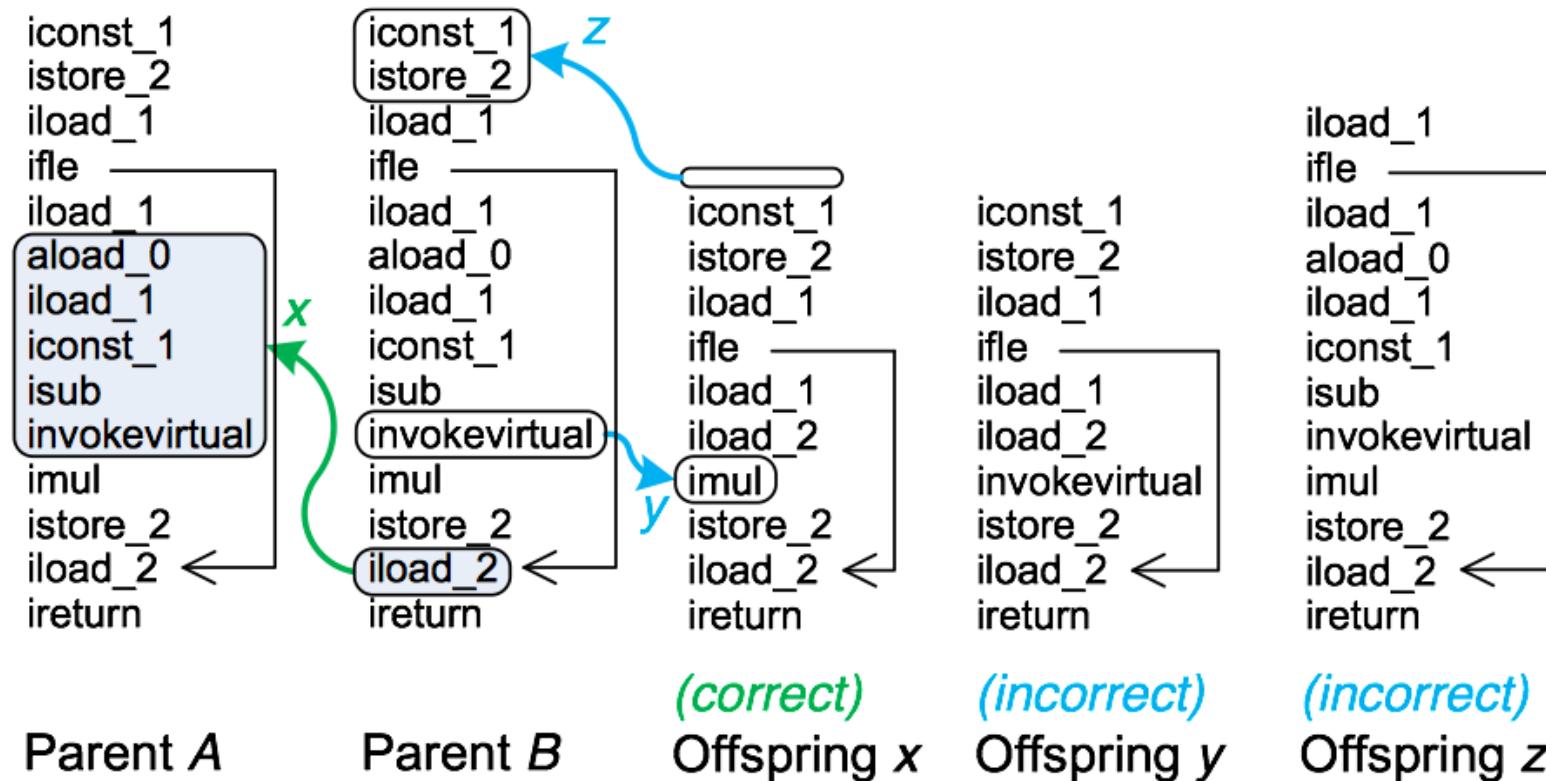


[http://link.springer.com/book/  
10.1007%2F978-0-387-31030-5](http://link.springer.com/book/10.1007%2F978-0-387-31030-5)

# Java Bytecode Example

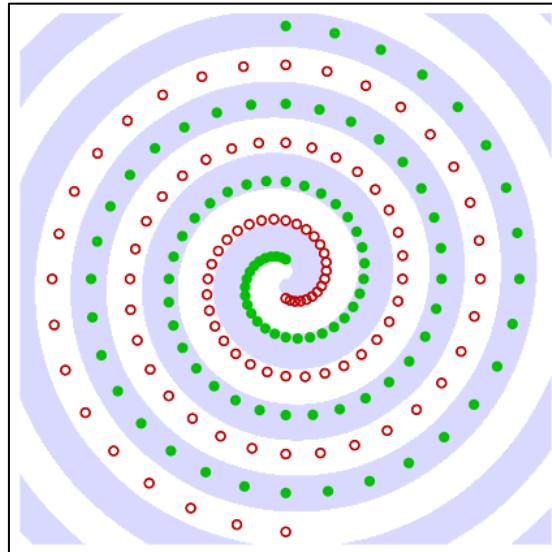
## ◊ FINCH [Orlov & Sipper 2010]

- ▷ Special crossover/mutation operators preserve type-compatibility and stack depth-compatibility:



# Java Bytecode Example

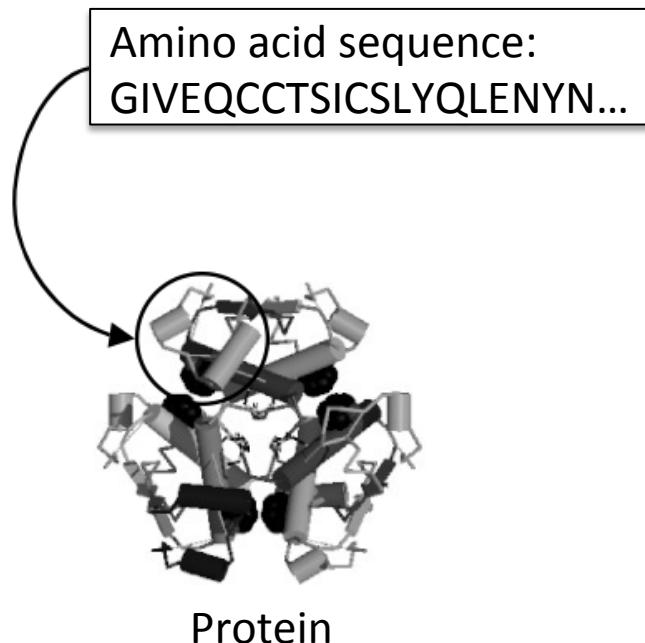
- ◊ Evolved bytecode programs can be converted to Java
  - ▷ e.g. Koza's intertwined spirals problem, which involves finding a classifier that can distinguish the points from two spirals:



```
boolean isFirst(double x, double y) {  
    double a, b, c, e;  
    a = Math.hypot(x, y);  e = y;  
    c = Math.atan2(y, b = x) +  
        -(b = Math.atan2(a, -a))  
        * (c = a + a) * (b + (c = b));  
    e = -b * Math.sin(c);  
    if (e < -0.0056126487018762772) {  
        b = Math.atan2(a, -a);  
        b = Math.atan2(a * c + b, x);  b = x;  
        return false;  
    }  
    else  
        return true;  
}
```

# Real World Example

- ❖ Protein localisation [Heddad et al. 2004]
  - ▷ Predicting which part of a cell a protein will be located in based upon patterns in its amino acid sequence



```
void gp(double *r, char *seq)
{
    r[3] = match("SA", seq);
    r[4] = match("[RK]R", seq);
    r[5] = match("[P]GP", seq);
    r[6] = match("[FWV]", seq);
    r[10] = match("[QS]", seq);

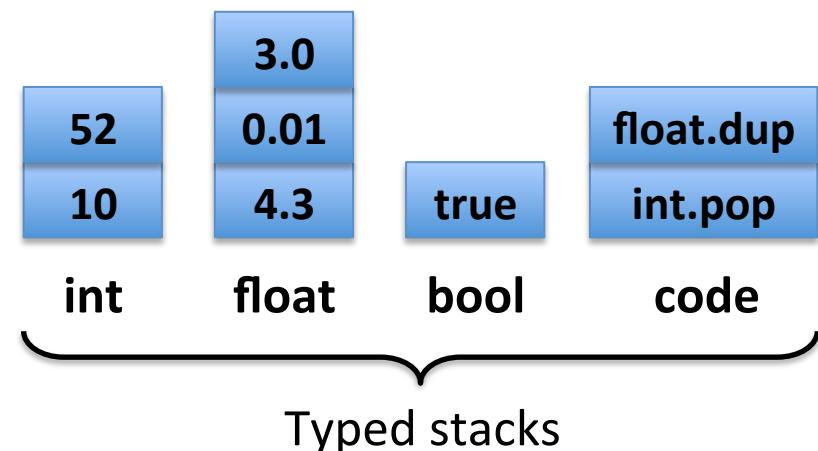
    r[3] = r[3] + r[5];
    r[8] = r[6] + r[3];
    r[0] = r[4] - r[8];
    r[0] = r[10] + r[0];
    r[0] = r[4] * r[0];
}
```

# Push

- ◊ A language designed for GP [Spector 2001]
  - ▷ <http://faculty.hampshire.edu/lspector/push.html>
  - ▷ A stack-based language, with one stack per type
  - ▷ Handles syntax and semantics in a flexible manner
  - ▷ Code stack can be used for modularity
  - ▷ Turing complete, relatively good evolvability

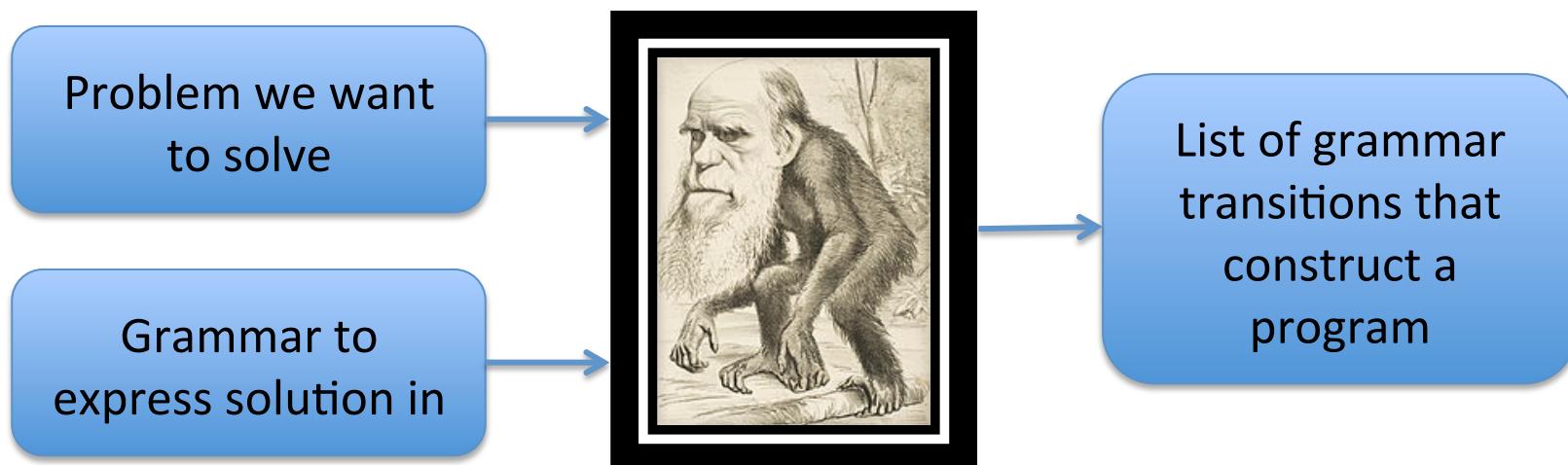
int.+ # 52 + 10, 62 goes on int stack  
code.do # calls float.dup (duplicate)  
float.\* # 3.0 \* 3.0, 9.0 on float stack

...



# Grammatical Evolution (GE)

- ❖ Evolves lists of grammar transitions [Ryan 1998]
  - ▷ Programming language is expressed by a grammar
  - ▷ Described in Backus Naur form
  - ▷ GE can then evolve any program in that grammar



# Grammatical Evolution (GE)

```
<exp> ::=      0<exp><op><exp> | 1(<exp><op><exp>) |  
                  2<pre-op>(<exp>) | 3<var>  
<op> ::=      0AND | 1OR | 2XOR  
<pre-op> ::= 0NOT  
<var> ::=      0IN1 | 1IN2 | 2IN3
```

Evolved chromosome:

10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---

# Grammatical Evolution (GE)

```
<exp> ::=  ^0<exp><op><exp> | ^1(<exp><op><exp>) |  
           ^2<pre-op>(<exp>) | ^3<var>  
<op> ::=   ^0AND | ^1OR | ^2XOR  
<pre-op> ::= ^0NOT  
<var> ::=   ^0IN1 | ^1IN2 | ^2IN3
```

Evolved  
<exp>

For the first step,  
start with the  
most general term

10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---

$$10 \bmod 4 = 2$$

Number of  
transitions in  
current  
grammar rule

Apply transition  
2 to the current  
term

# Grammatical Evolution (GE)

```
<exp> ::= 0<exp><op><exp> | 1(<exp><op><exp>) |  
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```

Evolved

&lt;exp&gt;

&lt;pre-op&gt;(&lt;exp&gt;)

For the first step,  
start with the  
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10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---

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```

Evolved

&lt;exp&gt;

&lt;pre-op&gt;(&lt;exp&gt;)

At each step, match  
the left-most  
unmatched term

10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---

$$18 \bmod 1 = 0$$

Number of  
transitions in  
current  
grammar rule

Apply transition  
0 to the current  
term

# Grammatical Evolution (GE)

```
<exp> ::= 0<exp><op><exp> | 1(<exp><op><exp>) |  
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<pre-op> ::= 0NOT  
<var> ::= 0IN1 | 1IN2 | 2IN3
```

Evolved

&lt;exp&gt;

&lt;pre-op&gt;(&lt;exp&gt;)

NOT(&lt;exp&gt;)

At each step, match  
the left-most  
unmatched term

10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---

$$18 \bmod 1 = 0$$

Number of  
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Apply transition  
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# Grammatical Evolution (GE)

```
<exp> ::= 0<exp><op><exp> | 1(<exp><op><exp>) |  
           2<pre-op>(<exp>) | 3<var>  
<op> ::= 0AND | 1OR | 2XOR  
<pre-op> ::= 0NOT  
<var> ::= 0IN1 | 1IN2 | 2IN3
```

Evolved chromosome:

10	18	41	27	6	39	21	47	13	31	19	8
----	----	----	----	---	----	----	----	----	----	----	---



$$41 \bmod 4 = 1$$

<exp>  
<pre-op>(<exp>)  
NOT(<exp>)  
NOT(<exp><op><exp>)  
...  
NOT(IN1 AND (IN2 OR IN3))

# Real World Example

## ❖ Evolving Super Mario levels [Shaker et al. 2012]

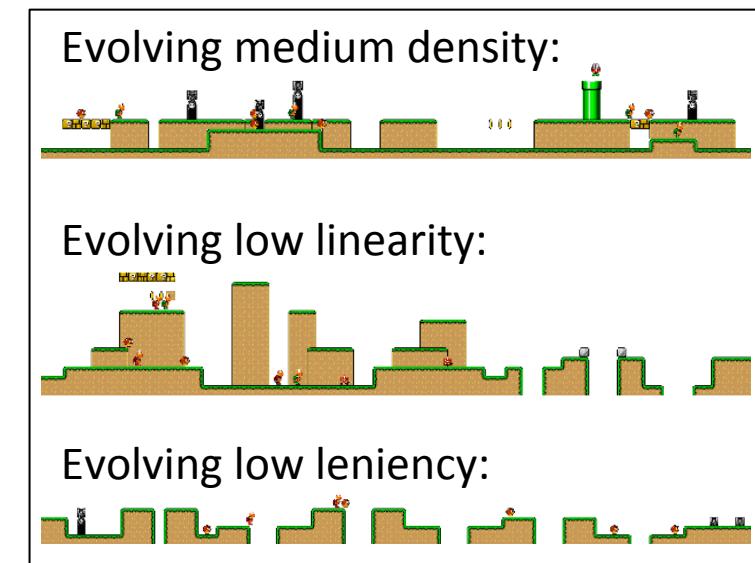
```

<level> ::= <chunks>  <enemy>
<chunks> ::= <chunk> | <chunk> <chunks>
<chunk> ::= gap(<x>, <y>, <wg>, <wbefore>, <wafter>)
           | platform(<x>, <y>, <w>)
           | hill(<x>, <y>, <w>)
           | cannon_hill(<x>, <y>, <h>, <wbefore>, <wafter>)
           | tube_hill(<x>, <y>, <h>, <wbefore>, <wafter>)
           | coin(<x>, <y>, <wc>)
           | cannon(<x>, <y>, <h>, <wbefore>, <wafter>)
           | tube(<x>, <y>, <h>, <wbefore>, <wafter>)
           | <boxes>

<boxes> ::= <box_type> (<x>, <y>)² | ...
           | <box_type> (<x>, <y>)⁶

<box_type> ::= blockcoin | blockpowerup
           | rockcoin | rockempty

<enemy> ::= (koopa | goomba) (<x>)² | ...
           | (koopa | goomba) (<x>)¹⁰
<x> ::= [5..95] <y> ::= [3..5]
  
```



# Grammatical Evolution (GE)

- ◊ A flexible and expressive approach
  - ▷ Since grammars can be defined for all languages
  - ▷ Programs have been evolved in C, for example
- ◊ Though modern languages are problematic
  - ▷ Complicated syntax and large APIs
  - ▷ Typically only a subset of a language is used
- ◊ Some concerns about evolvability
  - ▷ Sensitive to mutations at the left of a chromosome
  - ▷ These have a large effect upon the final expression

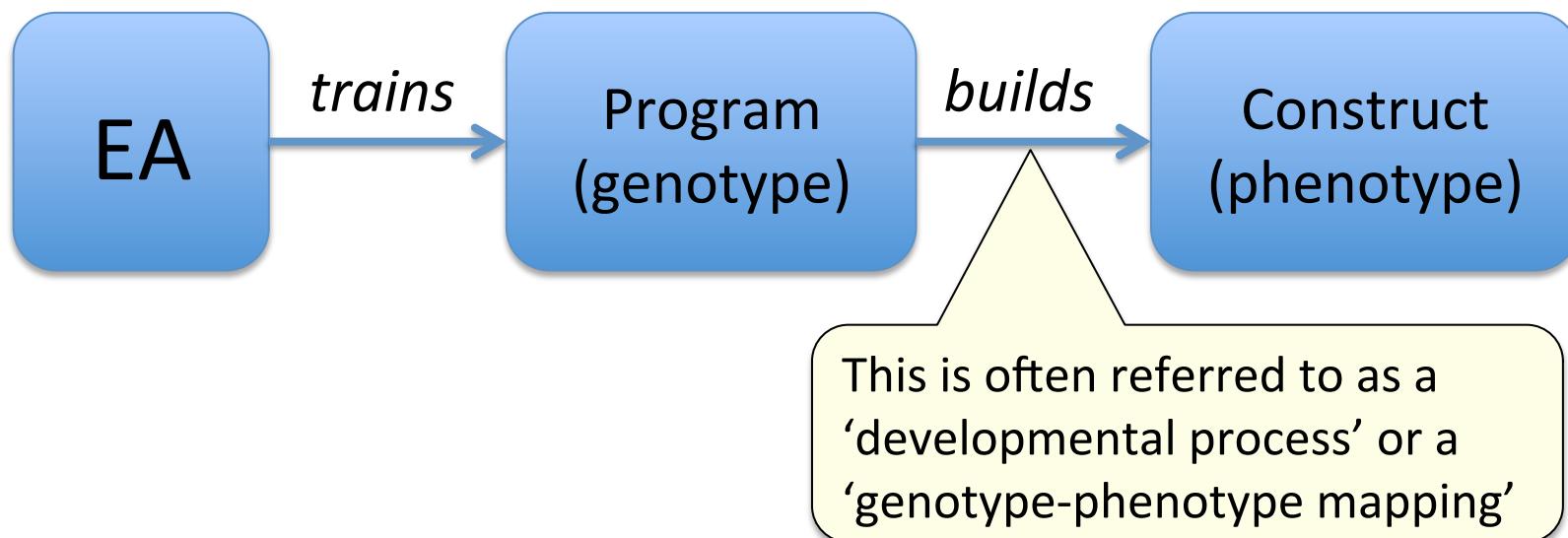
# Indirect Encodings

- ◊ Evolve something that constructs something else
  - ▷ Grammatical evolution does this, in a limited sense  
i.e. evolve grammar transitions that construct a program
  - ▷ You also saw it with genetic algorithms  
e.g. rule sets that construct bin packing solutions



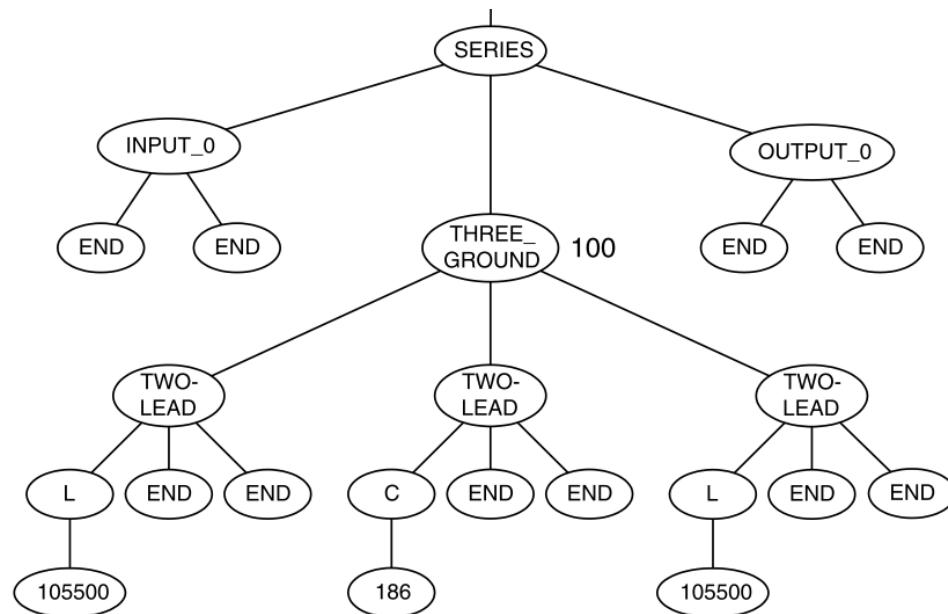
# Developmental GP

- ◊ Developmental GPs also use indirect encodings
  - ▷ Evolve programs that construct other entities, e.g. structures, circuits, or other programs
  - ▷ Often inspired by biological models of development
  - ▷ Often more scalable, able to solve bigger problems



# Koza's Developmental GP

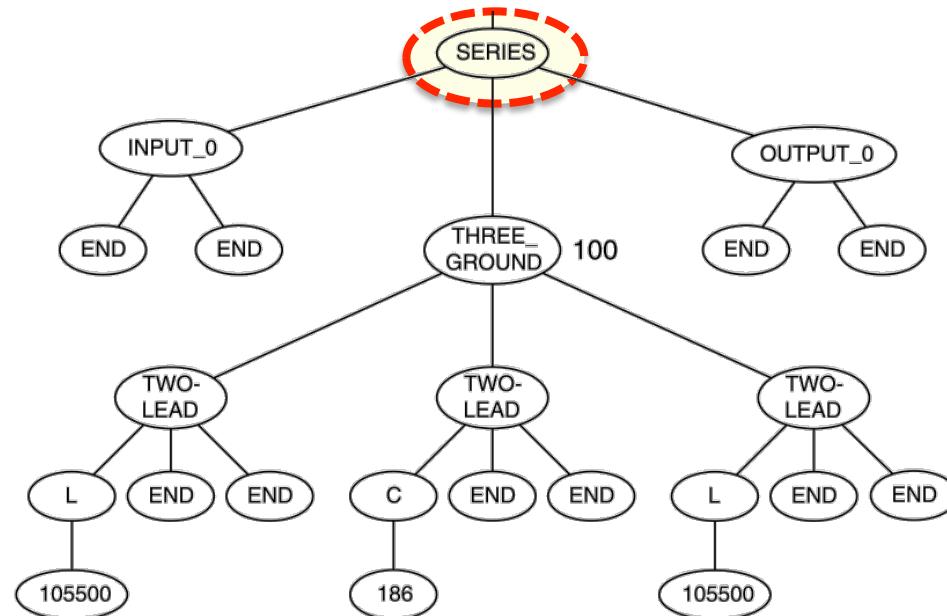
- ◊ Using tree-based GP to design circuits [Koza 2003]
  - ▷ This approach uses a GP tree to construct a graph
  - ▷ An early example of a developmental mapping



 Start here!

# Koza's Developmental GP

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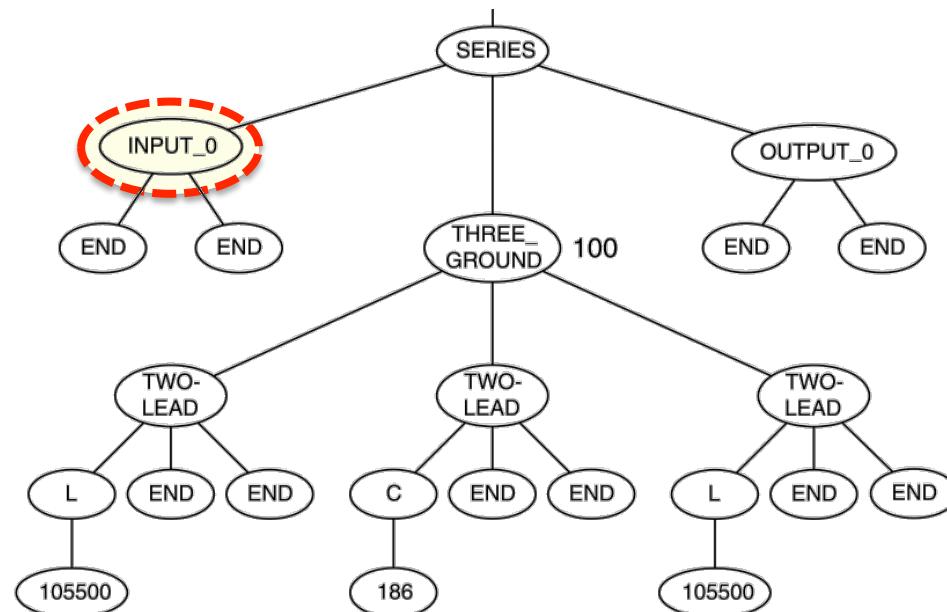


Create three nodes in series



# Koza's Developmental GP

- ◊ Using tree-based GP to design circuits [Koza 2003]
  - ▷ This approach uses a GP tree to construct a graph
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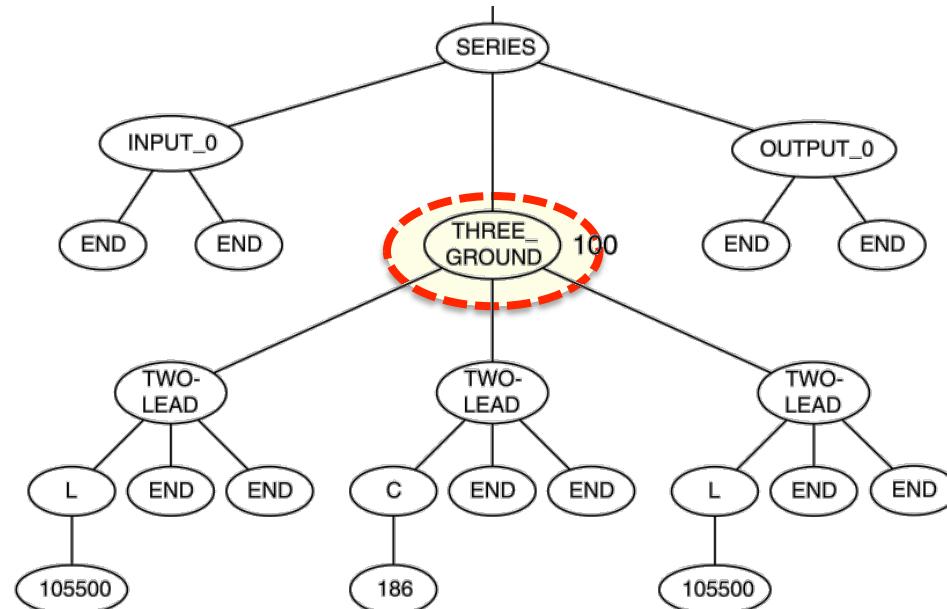


Instantiate first  
node

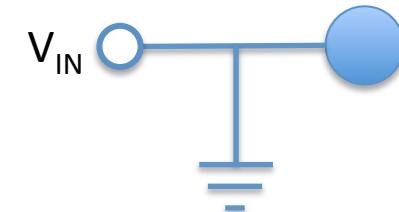


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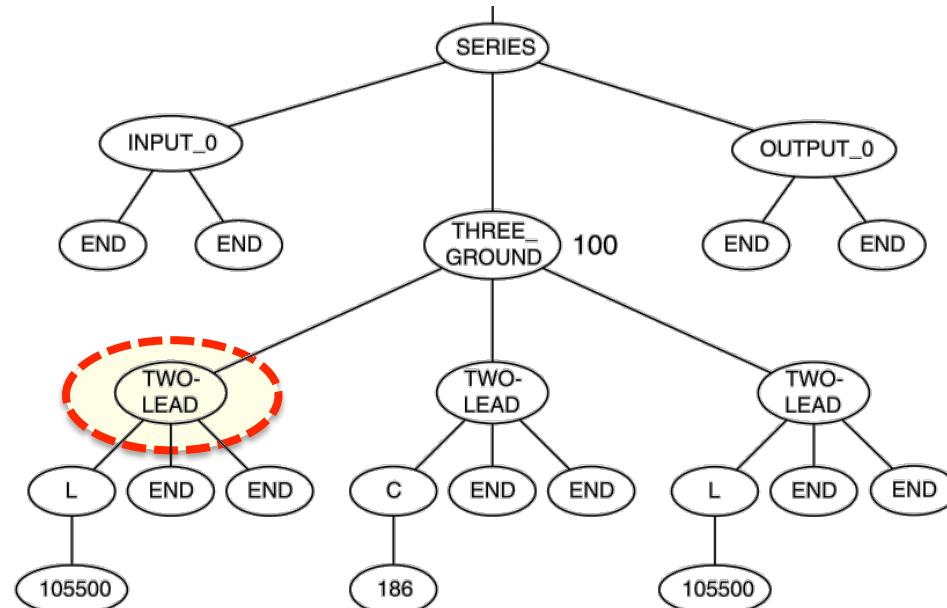


Add three-way link to ground

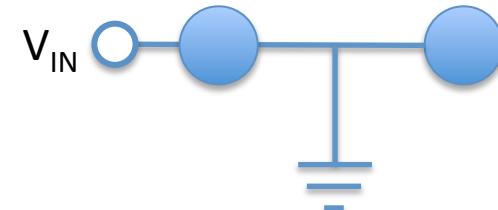


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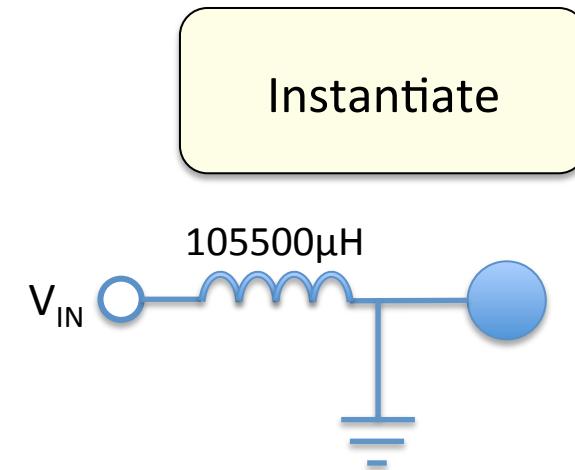
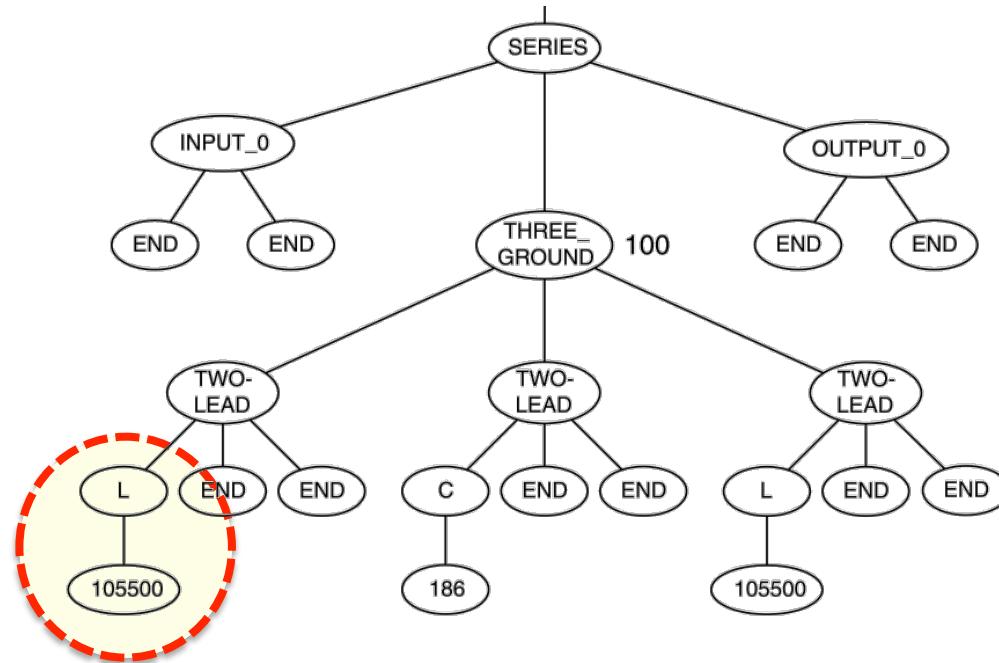


Add a node  
with two leads



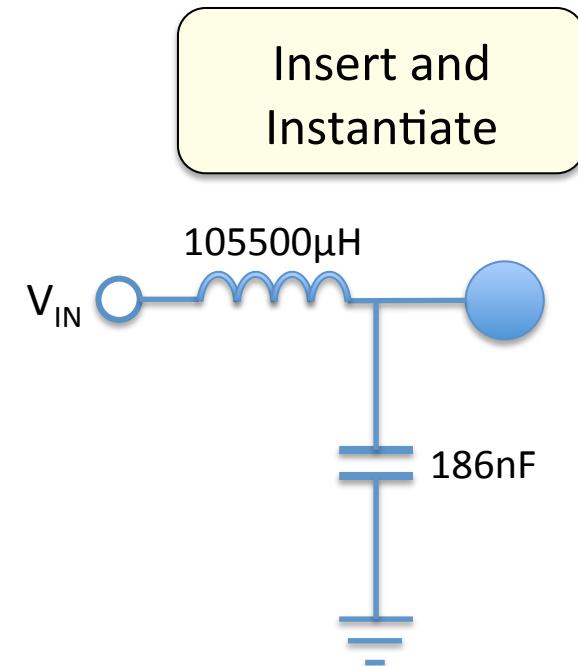
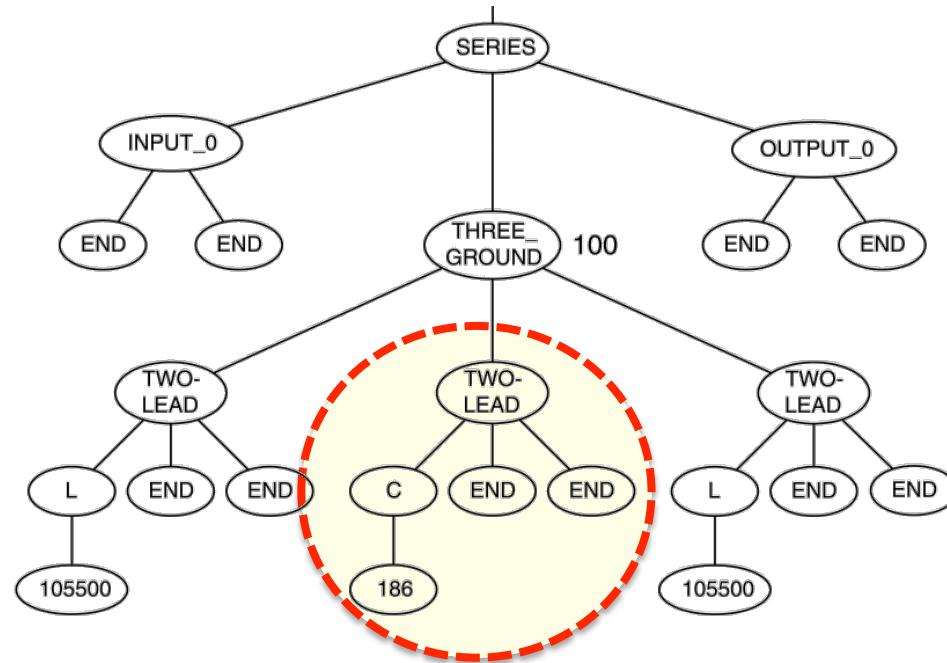
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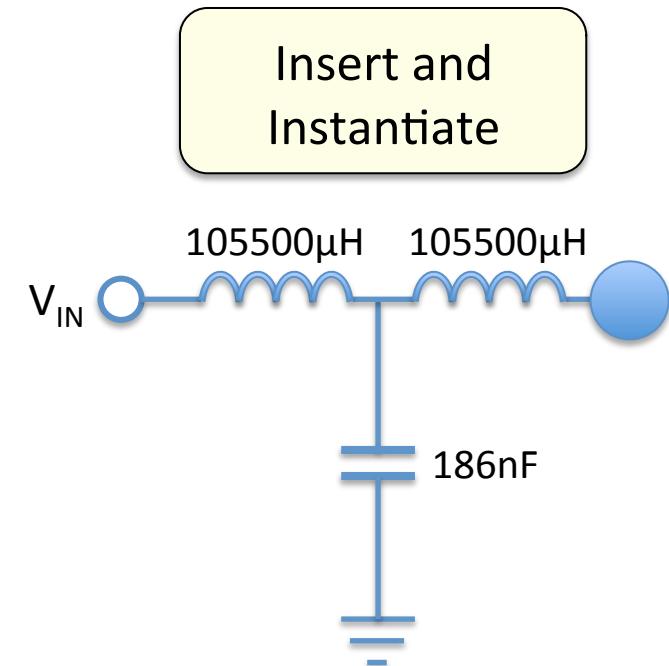
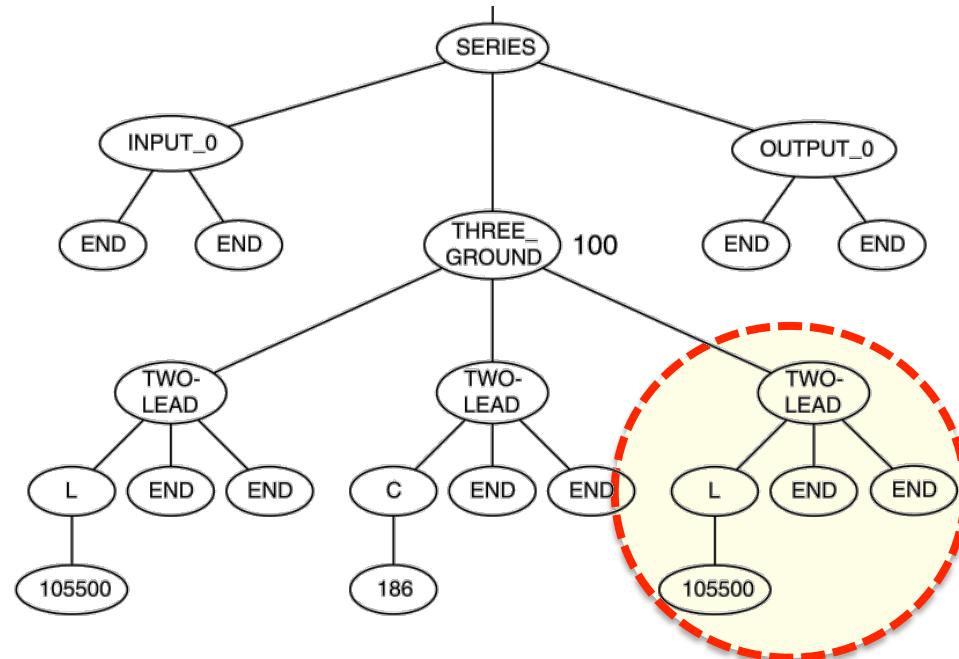
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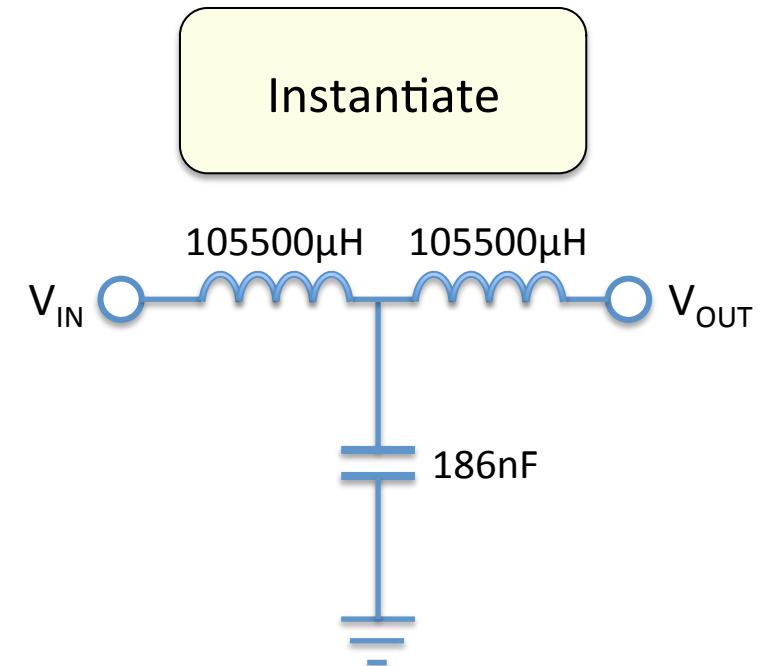
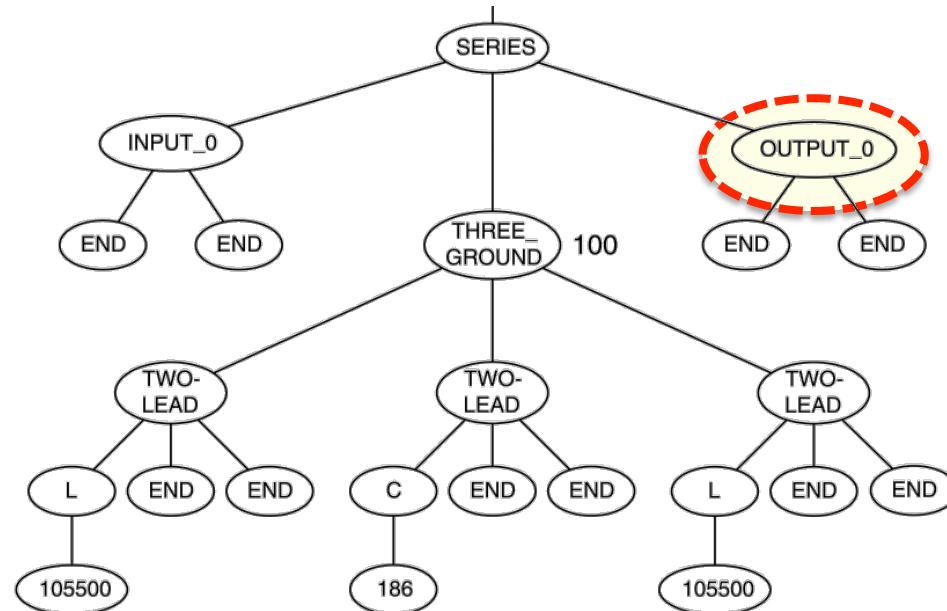
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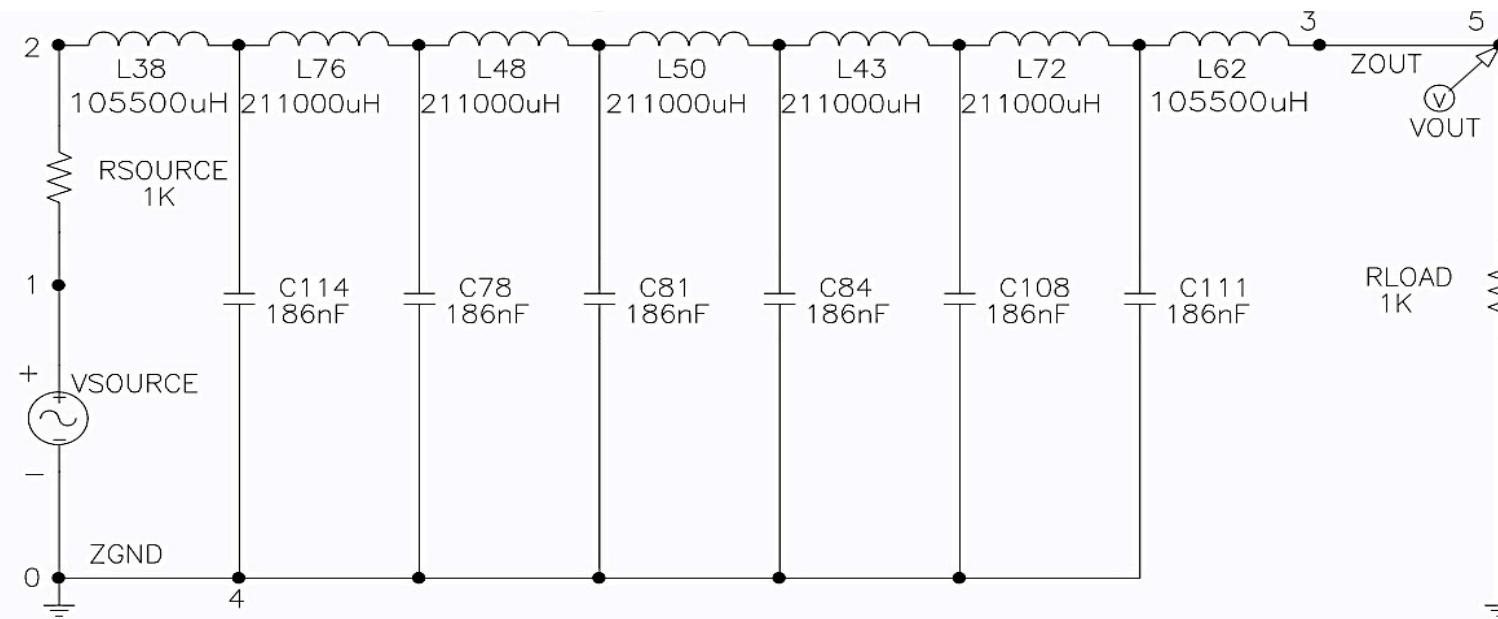
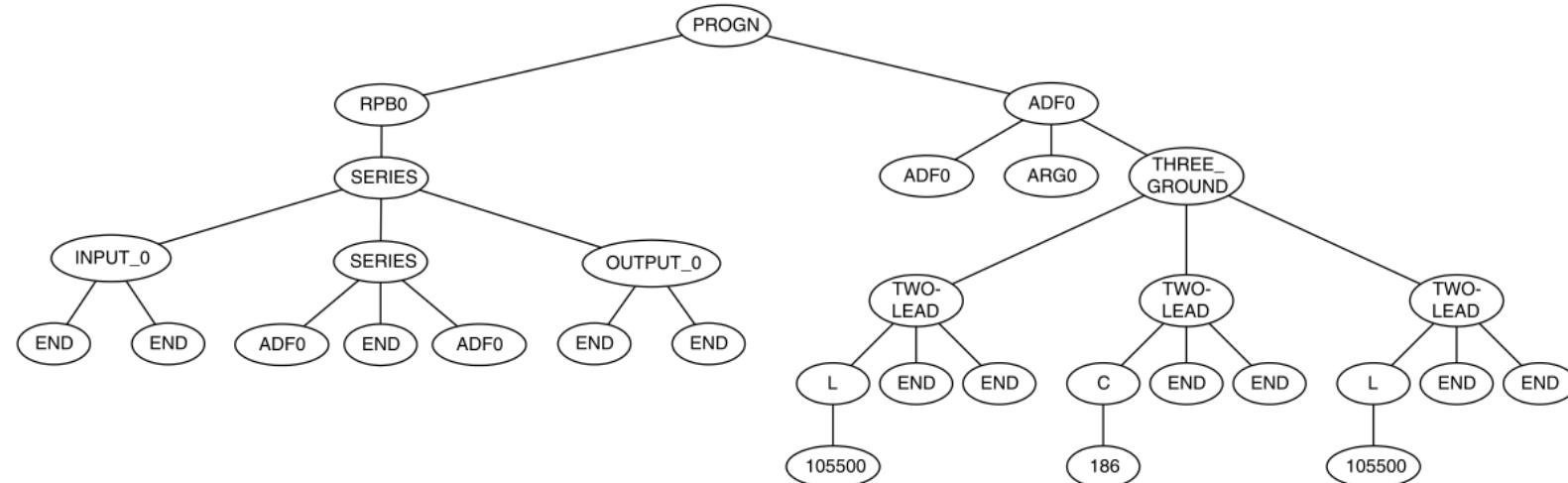


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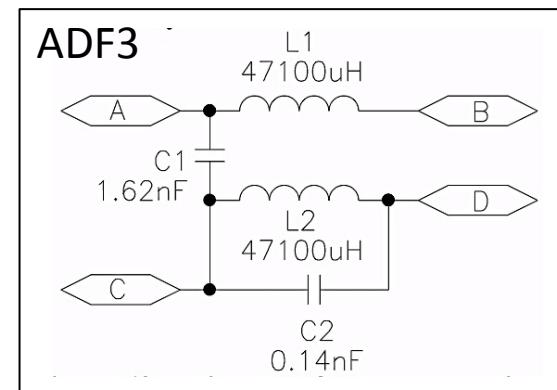
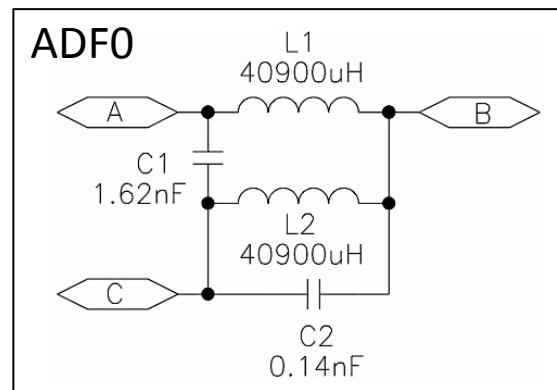
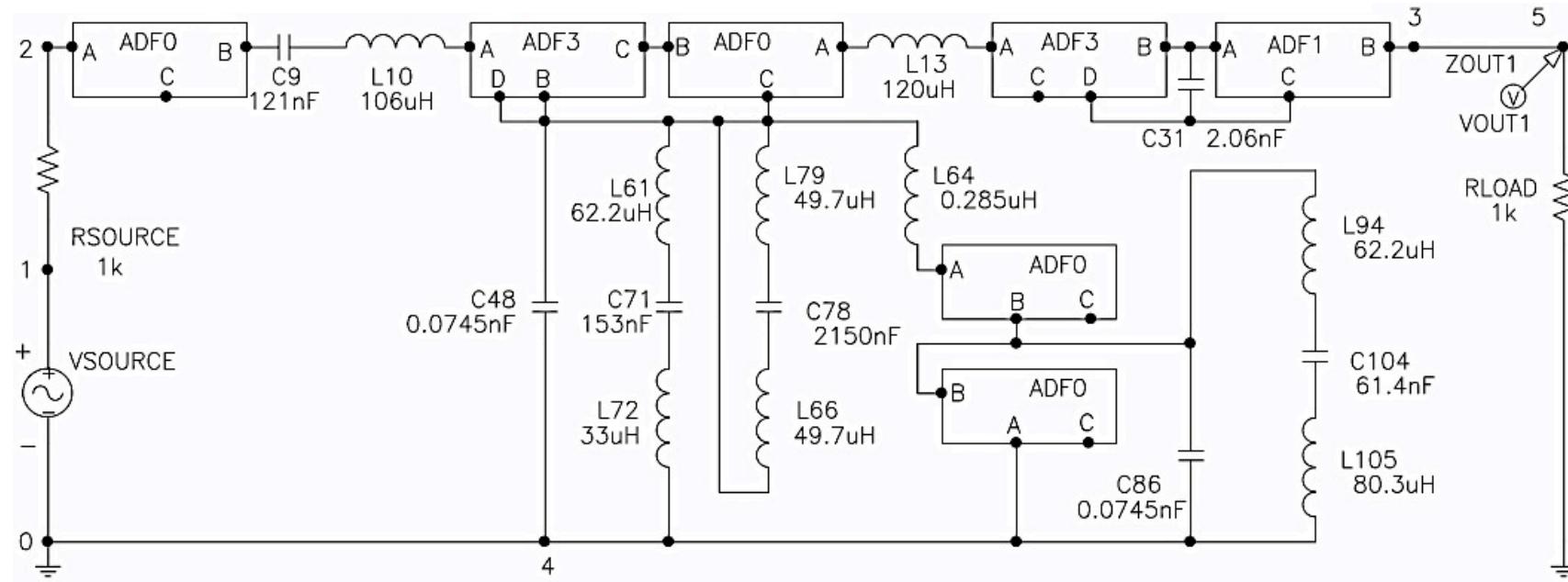
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# Modularity



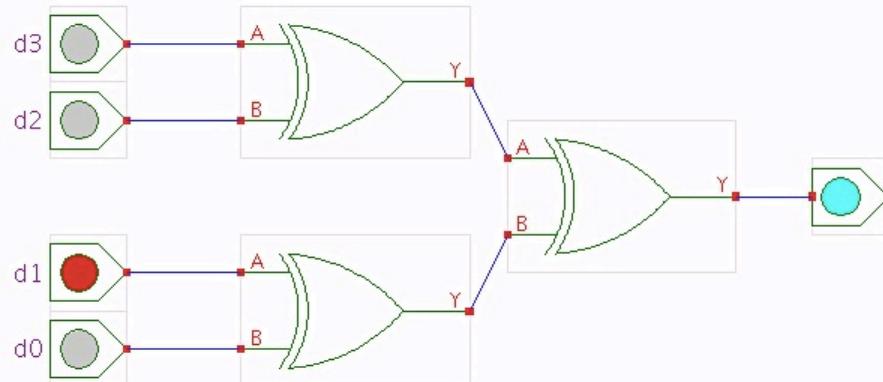
# Koza's Developmental GP



# Scalability

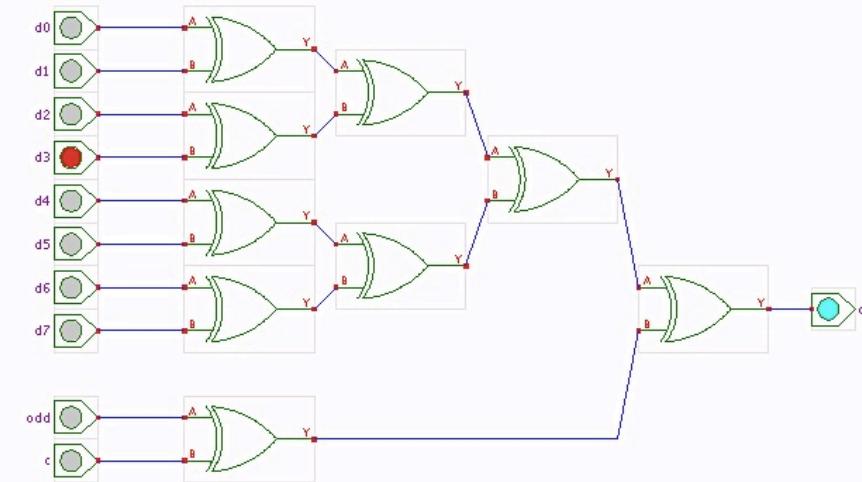
- ❖ Scalability is a problem for genetic programming
  - ▷ Search space grows exponentially with program size
  - ▷ Development allows programs to be compressed
  - ▷ Particularly when solutions have repetitive structure:

Even-4-parity circuit:



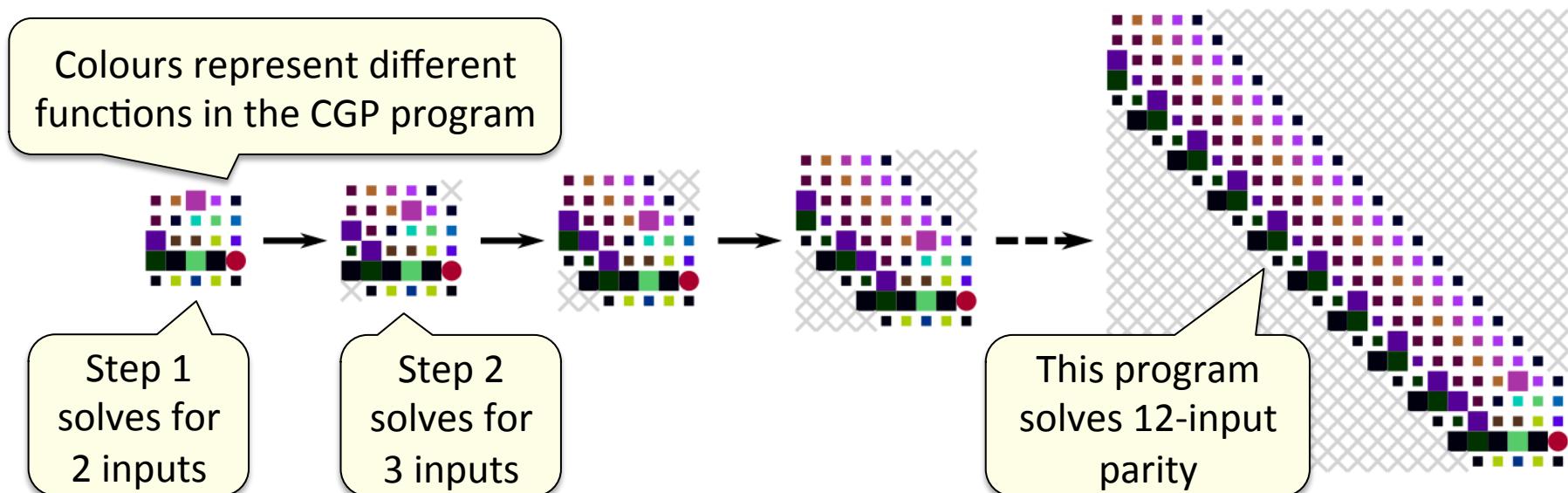
<http://tams-www.informatik.uni-hamburg.de/applets/hades/webdemos/index.html>

Even-8-parity circuit:



# Example: Self-Modifying CGP

- ◊ CGP programs that modify themselves [Harding'11]
  - ▷ Contains normal functions and self-modifying functions
    - E.g. delete nodes, duplicate nodes, change connection ...
  - ▷ A new program is created at each program iteration
    - Can generate general solutions, e.g. even-n-parity circuit:



# Autoconstructive Evolution

- ❖ Programs build their own offspring [Spector 2010]
  - ▷ i.e. they include code to copy and modify themselves
  - ▷ Based on the idea that programs can learn good patterns or regions of variation, for instance mutation hotspots
  - ▷ e.g. Autopush: autoconstructive evolution using Push
  - ▷ Modifies the program's "code" stack to construct a child

```
((integer.stackdepth (boolean.and code.map)) (integer.sub  
(integer.stackdepth (integer.sub (in (code.wrap (code.if (code.noop)  
Boolean.fromfloat (2) integer.fromfloat) (code.rand integer.rot)  
exec.swap code.append integer.mult))))))
```

Append to the  
code stack

Generate some  
random code

# Developmental GP

- ◊ A way of transitioning between representations
  - ▷ e.g. using a tree to represent a graph
  - ▷ Choose an evolvable representation, rather than one that is required by the problem domain
- ◊ Also a way of achieving scalability
  - ▷ Genotype space can be smaller than phenotype space
  - ▷ Human analogy: 30,000 genes encode 100 trillion cells
- ◊ And potentially for achieving complexity
  - ▷ Not limited to repetitive modular structures

# Things you should know

- ◊ Linear GP and grammatical evolution
  - ▷ How programs are represented
  - ▷ When they should be used, strengths and weaknesses
- ◊ Developmental GP
  - ▷ The meaning of indirect/developmental representation
  - ▷ Advantages over non-developmental GPs
- ◊ I don't expect you to know
  - ▷ Low-level details, e.g. translating a GE expression
  - ▷ Push, the different kinds of developmental GP

# What's Next?

- ❖ Biological representations of computation
  - ▷ Most of the approaches discussed so far use conventional representations of computation
  - ▷ Conventional representations are fragile
  - ▷ Developmental GP hints at the potential of representing computation in unconventional ways
  - ▷ *This is the topic of the next few lectures...*
- ▷ Next week: Cellular Automata
  - Complex behaviour from simple systems

# Things to try out

- ◊ Have a look at Grammatical Evolution
  - ▷ `ec(gp,ge)` package in ECJ
  - ▷ <http://cs.gmu.edu/~eclab/projects/ecj/docs/manual/manual.pdf>
    - See section 5.3
- ◊ Have a look at Push
  - ▷ `ec(gp,push)` package in ECJ
  - ▷ <http://cs.gmu.edu/~eclab/projects/ecj/docs/manual/manual.pdf>
    - See section 5.4

# Bibliography

- ◊ S. Harding et al, SMCGP2: self modifying Cartesian genetic programming in two dimensions, GECCO 2011  
<http://www.cartesiangp.co.uk/papers/gecco2011a-harding.pdf>
- ◊ A. Heddad et al, Evolving Regular Expression-based Sequence Classifiers for Protein Nuclear Localisation, EvoBIO 2004  
<http://www.sbc.su.se/~maccallr/publications/hedad-evobio2004.pdf>
- ◊ J. Koza et al., The Importance of Reuse and Development in Evolvable Hardware, 2003 NASA/DoD Conference on Evolvable Hardware, 2003  
<http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.118.5365>
- ◊ M. Orlov and M. Sipper, Flight of the FINCH Through the Java Wilderness, IEEE TEvC 15(2), 2011  
<http://finch.cs.bgu.ac.il/pubs/finch.pdf>
- ◊ C. Ryan, Grammatical Evolution: Evolving Programs for an Arbitrary Language, EuroGP 1998, <http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.38.7697>
- ◊ N. Shaker et al, Evolving Levels for Super Mario Bros Using Grammatical Evolution, CIG2012, <http://noorshaker.com/docs/ELGE.pdf>
- ◊ L. Spector, Towards Practical Autoconstructive Evolution: Self-Evolution of Problem-Solving Genetic Programming Systems, GPTP VIII, 2010.  
<http://faculty.hampshire.edu/lspector/pubs/spector-gptp10-preprint.pdf>